

Title

Effect of shift in refractive index of dispersive elements in waveband-shift-free optical phase conjugator based on DFG

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Abstract

In this study, the effect of the shift in the refractive index between two dispersive elements on the output phase-conjugated (PC) wave power of waveband-shift-free optical-phase conjugators based on difference-frequency generation (DFG-OPCs) is analyzed. First, a numerical model of the DFG-OPC is built by considering the shift Δn in the refractive index. The derived formula shows that the output PC wave power of DFG-OPCs depends on the shift in the refractive index. Subsequently, the dependence of the output PC wave power on the shift is confirmed analytically. Calculations indicate that the output PC wave power varies according to the shift. For a relatively fractional shift $\Delta n = 1.0 \times 10^{-6}$, the output PC power is degraded by 3 dB. Finally, acceptable values of the shift and temperature difference are calculated as functions of the length of the dispersive element. It is illustrated in this study that the acceptable value of shift in the refractive index increases as the length of the dispersive element is reduced and that the output PC wave power can be stabilized against changes in temperature.

Keywords

Optical Nonlinear Compensation, Optical Phase Conjugation, Waveband-Shift-Free, Difference-Frequency Generation, Refractive Index Shift, Dispersive Elements

Declarations

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The data that support the findings of this study are available from the corresponding author upon reasonable request.

Code availability (software application or custom code)

The data that support the findings of this study are available from the corresponding author upon reasonable request.

1. Introduction

To accommodate the increase in Internet traffic, higher speed and spectrally efficient optical fiber communication systems are required [1]. One factor that limits high-speed optical fiber transmission is the optical nonlinear degradation caused by the nonlinearity of the fiber [2, 3]. Optical nonlinear compensation using digital signal processing (DSP) algorithms, e.g., digital backpropagation [4, 5], Volterra series transfer function [6], and artificial neural networks [7, 8], are successful technologies that can mitigate degradations in signals caused by optical nonlinearity. For further improvement in the quality of the received signal, the combination of a DSP technique and an optical signal processing (OSP) technique is beneficial. Non-degenerate phase-sensitive optical amplifiers (PSAs) have recently received broad attention because not only low-noise amplification but also nonlinear phase noise compensation can be achieved in the optical domain [9-13]. However, the PSAs require phase-conjugated twin wave transmission [14] which halves spectral efficiency (SE). In the meantime, optical phase conjugator (OPC) [15-26] is based on an OSP technique and has the potential to reduce the computational cost of receiver-side DSP calculations. This is because the signal degradations caused by chromatic dispersion and optical nonlinearity are simultaneously compensated by the OPC in the optical domain and contribute to reducing the computational load on receiver-side DSP. An OPC is placed in the middle of the transmission fibers, where it generates a phase-conjugate (PC) wave of a signal wave transmitted through the first half of the span. The generated PC wave includes inverted distortion arising from linear and nonlinear impairments in the first half of the span and is launched into the second half of the span. After transmission, the distortions of the first and second halves of the spans are canceled. However, in conventional OPCs, the wavelengths of the PC waves are shifted from those of the signal waves during generation [15]. Therefore, a waveband must be reserved for the PC waves, and this leads to the degradation of SE. Recently, waveband-shift-free OPCs, which generate spectrally inverted PC waves of the incoming wavelength-division multiplexed (WDM) signal waves at the same center wavelength as that of the WDM signal waves, have been demonstrated to mitigate the degradation of the SE [16-22]. Such OPCs are classified into two types—one based on four-wave mixing (FWM) and the other based on difference-frequency generation (DFG). The FWM-based OPCs [16-20] employ dual pumps for PC wave generation and require guard bands to avoid nonlinear crosstalk among the incoming WDM signal waves via the pumps. This leads to the degradation of the SE. Furthermore, it is difficult to generate PC waves from broad WDM signal waves owing to phase matching in an optical $\chi^{(3)}$ nonlinear medium for FWM. The DFG-based OPCs enable broadband PC wave generation because of the optical $\chi^{(2)}$ nonlinear medium for DFG [21, 22]. In the experimental demonstration [21], only a 25-GHz guard band is required at the center channel of the WDM signal waves. However, there is still scope to improve the SE and its configuration, including wavelength-selective switches. On the other hand, we propose and numerically investigate waveband-shift-free OPC based on DFG

(DFG-OPC) [23], which is inspired by the studies [24, 25]. The DFG-OPC does not require the guard band of the center channel of the WDM signal waves and is composed of a Sagnac loop interferometer (SLI), including an optical nonlinear medium and dispersive elements (DEs). The signal and pump wave are launched into the SLI, and a PC wave with the same center wavelength as the signal wave is generated by an optical $\chi^{(2)}$ nonlinear medium such as a periodically poled lithium niobate (PPLN) waveguide. Subsequently, PC waves generated from the input waves with clockwise and counterclockwise rotation interfere with a specific phase difference caused by the DEs, and only the PC wave is output from the output port.

In our previous study [23], it was assumed that the phase constants between two DEs were identified. However, in reality, the refractive indexes of the DEs change owing to fluctuations in temperature, which affect the output PC wave power. In the conference paper [26], as an initial verification step, we have analytically studied the effect of the shift in the refractive indexes of the DEs in a DFG-OPC circuit, and the degradation in the output PC wave power owing to the shift in the refractive index has been confirmed. However, quantitative evaluations have been insufficient, and the relationship between the degradation in the output PC wave power and the shift in the refractive indexes of the DEs has not been clarified in detail.

This study is an extension of [26]. First, we mathematically show the effect of the shift in the refractive indexes between the DEs on the DFG-OPC circuit and calculate the output PC wave power as a function of the difference in the lengths of the DEs under circumstances in which the shift is not equal to zero. Thereafter, it is numerically investigated that degradation of the output PC power depends on the shift in the refractive indexes. Finally, an acceptable value of the shift in the refractive indexes of the DEs is determined to obtain stable output PC wave power from DFG-OPCs. In this paper, standard single-mode fibers (SSMFs) are assumed to be used as DEs even though there are many types of DEs such as silicon, polymer, silica, and lithium niobate waveguides. This is because the SSMFs are well compatible with the fiber-pigtailed components which would be used for the future experimental demonstration of DFG-OPC.

2. Mathematical expression of effect of refractive index on DFG-OPCs

In the DFG-OPC, a PC wave with the maximum power can be obtained when the phase difference between the clockwise and counterclockwise propagating PC waves generated in an SLI is appropriately adjusted using DEs. However, the phase shift for the PC waves is determined by not only the lengths of the DEs but also the phase constants of the DEs, depending on the refractive indexes of the DEs and the wavelengths of the PC waves. Therefore, there is a concern that the output PC wave power will decrease owing to the shift in the refractive indexes between the DEs. In this section, we formulate the effect of this shift on the output PC wave power.

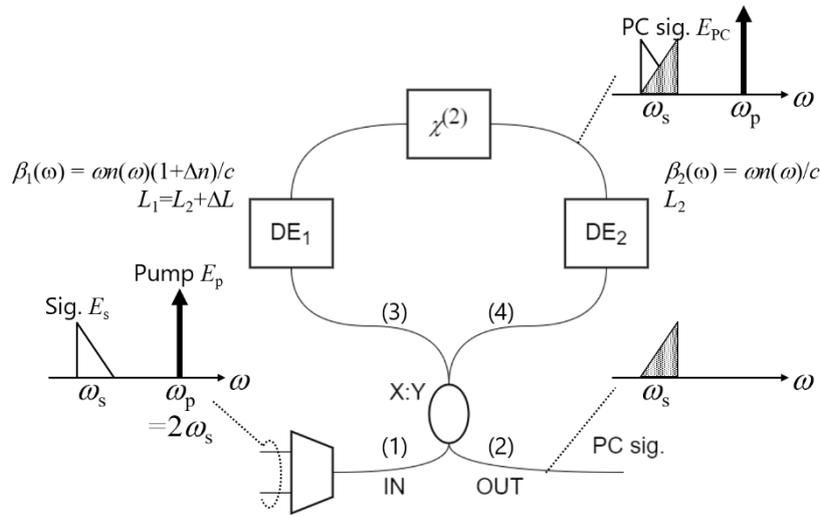


Fig. 1 DFG-OPC model

Figure 1 presents the schematic of a DFG-OPC enabling waveband-shift-free PC wave generation. As depicted in Fig. 1, the DFG-OPC is composed of an SLI consisting of an optical 3-dB coupler (CPL), two DEs, and a $\chi^{(2)}$ optical nonlinear material. First, a signal and pump waves with complex electric field amplitudes E_s and E_p are input to port 1 of the CPL. Here, the central optical angular frequencies of the signal and pump waves are ω_s and $\omega_p (=2\omega_s)$, respectively. These waves are divided into two parts and output from ports 3 and 4, respectively, of the CPL. For the clockwise propagation of the SLI, the signal and pump waves are phase-shifted by DE₁ with a phase constant $\beta_1(\omega) (= n_1(\omega)\omega/c)$ and length L_1 . Thereafter, the phase-shifted signal and pump waves are guided into $\chi^{(2)}$ optical nonlinear material such as a PPLN waveguide, and PC waves, E_{PC} , with an optical angular frequency $\omega_{PC} = \omega_p - \omega_s$ are generated through the DFG process. The DFG process can be expressed as the following analytical solution of mode-coupled equations under the assumption that pump depletion and $\chi^{(2)}$ waveguide loss are negligible [27]:

$$\begin{cases} E_s(z) e^{j\Delta kz/2} = E_s(0) \left[\cosh(sz) + \frac{j\Delta k}{2s} \sinh(sz) \right] - j \frac{g}{2s} E_{PC}^*(0) \sinh(sz) \\ E_{PC}^*(z) e^{-j\Delta kz/2} = E_{PC}^*(0) \left[\cosh(sz) - \frac{j\Delta k}{2s} \sinh(sz) \right] + j \frac{g}{2s} E_s(0) \sinh(sz) \end{cases} \quad (1)$$

In Eq. (1), the phase mismatching coefficient Δk can be expressed as $\Delta k = |k_p - k_s - k_{PC}| - 2\pi/\Lambda$, where k_p , k_s , and k_{PC} and Λ are the phase constants of the pump, signal, and PC waves and the polarization-inverted period for quasi-phase matching, respectively. The gain coefficient $g = \kappa E_p(0)$, where κ is the coupling coefficient. Further, $s = \sqrt{|g/2|^2 - (\Delta k/2)^2}$. Therefore, the PC, signal, and pump

waves are phase-shifted by DE₂ with a phase constant $\beta_2(\omega)$ and length L_2 and input to port 4 of the CPL. Similarly, the PC, signal, and pump waves propagating counterclockwise of the SLI are input to port 3 of the CPL and made to interfere with the clockwise propagating waves. The output PC wave power from ports 1 and 2 of the CPL can be described as follows:

$$\begin{aligned} P_{PC1} &\propto \left| \frac{E_{CCW}^{PC}}{\sqrt{2}} - \frac{jE_{CW}^{PC}}{\sqrt{2}} \right|^2 \\ &= P_{PC} + P_{PC} \sin \left[\left\{ \beta_2(\omega_p) - 2\beta_2(\omega_s) \right\} L_2 - \left\{ \beta_1(\omega_p) - 2\beta_1(\omega_s) \right\} L_1 \right] \end{aligned} \quad (2)$$

$$\begin{aligned} P_{PC2} &\propto \left| \frac{E_{CW}^{PC}}{\sqrt{2}} - \frac{jE_{CCW}^{PC}}{\sqrt{2}} \right|^2 \\ &= P_{PC} - P_{PC} \sin \left[\left\{ \beta_2(\omega_p) - 2\beta_2(\omega_s) \right\} L_2 - \left\{ \beta_1(\omega_p) - 2\beta_1(\omega_s) \right\} L_1 \right] \end{aligned} \quad (3)$$

Here, E_{CW}^{PC} and E_{CCW}^{PC} denote the complex electric field amplitude of the PC waves with clockwise and counterclockwise propagation, and $P_{PC} = \kappa^2 |E_s E_p|^2 \sinh^2(sz) / 16s^2$. Subsequently, we introduce the shift in the refractive index, $\Delta n (= n_1/n_2 - 1)$, between the two DEs and the difference in DE lengths, $\Delta L (= L_1 - L_2)$, and substitute them to Eqs. (2) and (3). Therefore,

$$P_{PC1} \propto P_{PC} + P_{PC} \sin \left[\left\{ 2\beta_2(\omega_s) - \beta_2(\omega_p) \right\} \left\{ \Delta L + \Delta n(L_2 + \Delta L) \right\} \right] \quad (4)$$

$$P_{PC2} \propto P_{PC} - P_{PC} \sin \left[\left\{ 2\beta_2(\omega_s) - \beta_2(\omega_p) \right\} \left\{ \Delta L + \Delta n(L_2 + \Delta L) \right\} \right] \quad (5)$$

Here, P_{PC2} is the PC wave power from port 2 of the CPL, i.e., the desired DFG-OPC output. As expressed by Eqs. (4) and (5), the effect of the shift in the refractive index between the two DEs in

DFG-OPCs on the output PC wave power is formulated. When $[\{2\beta_2(\omega_s) - \beta_2(\omega_p)\}\{\Delta L + \Delta n(L_2 + \Delta L)\}] = -\pi/2 + 2\pi N$ ($N = 0, 1, 2, \dots$), the DFG-OPC output P_{PC2} can be maximized. In the case of $\Delta n = 0$, the maximum DFG-OPC output power can be obtained through the adjustment of the difference in DE lengths, ΔL , appropriately. However, in the case of $\Delta n \neq 0$, the DFG-OPC output P_{PC2} depends not only on ΔL but also on Δn and L_2 . The effect of parameters such as Δn and L_2 on the output PC wave power should be studied in detail because it seems difficult to manage the shift Δn in the refractive index with respect to the temperature.

3. Dependence of output PC wave power on shift in refractive indexes between DEs

In this section, the dependence of the output PC wave power on the difference in DE lengths, ΔL , in the presence of the shift Δn in the refractive index and the dependence of the output PC wave power on Δn are examined.

The simulation model is the same as that depicted in Fig. 1. The calculation conditions and parameters are basically identified as done in [14], except for Δn and L_2 . For the input waves, the wavelength λ_s and power of the signal wave E_{s2} are 1550 nm and 1 μ W, respectively. Thus, the wavelength λ_p and power of the pump wave E_{p2} are 775 nm and 350 mW, respectively. For the DFG-OPC configuration, the splitting ratio of the CPL is 50:50. We assume that a PPLN waveguide is employed as the $\chi^{(2)}$ optical nonlinear material. Its parameters are waveguide length of 5 cm, coupling coefficient $\kappa = 63 \text{ W}^{-1/2}\text{m}^{-1}$, and polarization inverted period for quasi-phase matching, $\Lambda = 23.9 \text{ }\mu\text{m}$, for $\Delta k = 0$. In addition, the Sellmeier dispersion formula is used to consider dispersion in the PPLN waveguide [28]. The DEs are assumed to be conventional optical fibers. Their phase constant $\beta(\omega)$ is defined as $\beta(\omega) = n(\omega)\omega/c$, where c is the speed of light and the refractive index of the optical fiber $n(\omega)$ is expressed by the experimental formula described in [27]. As described in Section 2, the difference in length between the DEs is $\Delta L = L_1 - L_2$ and the shift in the refractive indexes between the DEs is $\Delta n = n_1/n_2 - 1$.

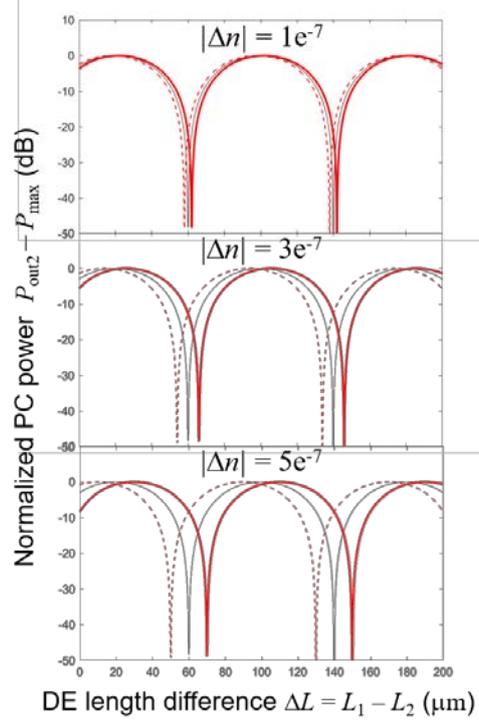


Fig. 2 Normalized output PC wave power $P_{\text{out}2} - P_{\text{max}}$ as a function of difference in DE lengths, ΔL . Black solid lines indicate $\Delta n = 0$ and dashed and bold solid red lines indicate $+\Delta n$ and $-\Delta n$

Figure 2 depicts the dependence of the output PC wave power on the difference in DE lengths, ΔL , when the shift in the refractive index, $\Delta n \neq 0$. In each graph, the horizontal axis represents the difference in DE lengths, ΔL , and the vertical axis represents the normalized output PC wave power, defined as $P_{\text{PC}2} - P_{\text{max}}$, where P_{max} is the maximum output PC wave power. The black lines represent the case $\Delta n = 0$. The bold solid red and dashed red lines represent the cases $+\Delta n$ and $-\Delta n$. Figure 2 is calculated for the case $L_2 = 20$ m, and the top, middle, and bottom figures represent the cases $|\Delta n| = 1e^{-7}$, $3e^{-7}$, and $5e^{-7}$, respectively. When $\Delta n = 0$, the maximum output PC wave power is obtained at $\Delta L = 20, 100, \text{ and } 180 \mu\text{m}$. However, as $|\Delta n|$ increases, the value of ΔL taking the maximum output PC wave power is changed. Therefore, the output PC power at $\Delta L = 20, 100, \text{ and } 180 \mu\text{m}$ is degraded. For the quantitative evaluation of this phenomenon, the degradation in the output PC wave power, ΔP , is calculated as a function of the shift, Δn , in the refractive index. Figure 3(a) presents the results of the calculation. As depicted in the inset of Fig. 3(a), the degradation ΔP in the output PC wave power is defined as $\Delta P = P_{\text{max}} - P_{\text{out}2}$ at $\Delta L_{\text{opt}} = 20 \mu\text{m}$. The degradation ΔP in the PC optical power increases with the increase in $|\Delta n|$ and displays a convex-function-like trend. Figure 3(b) presents another version of Fig. 3(a), in which the horizontal axis ranges from $-10e^{-6}$ to $+10e^{-6}$. Several peaks can be identified for each DE₂ length, $L_2 = 5, 10, \text{ and } 20$ m. This is evident from Fig. 2. When $|\Delta n|$ increases, the curve of the output PC wave power shifts. Finally, the value of

this output power reduces to the minimum, although $\Delta L = 20 \mu\text{m}$. Therefore, the degradation ΔP in the PC wave power has local maximum values. It can be seen from Fig. 3(b) that DE_2 with length significantly shorter than 5 m is preferred to avoid degradation in the output PC wave power when the temperature difference between the two DEs is $1.0 \text{ }^\circ\text{C}$. This is because there are local maximum values located near $\Delta n = \pm 8.0 \times 10^{-6}$ corresponding to the thermo-optical coefficient of $7.814 \times 10^{-6}/^\circ\text{C}$ for single-mode fibers [29]. This result indicates that there is a fair chance for the reduction of the degradation in the output PC wave power caused by the shift in the refractive index (temperature fluctuation) by reducing L_2 as much as possible

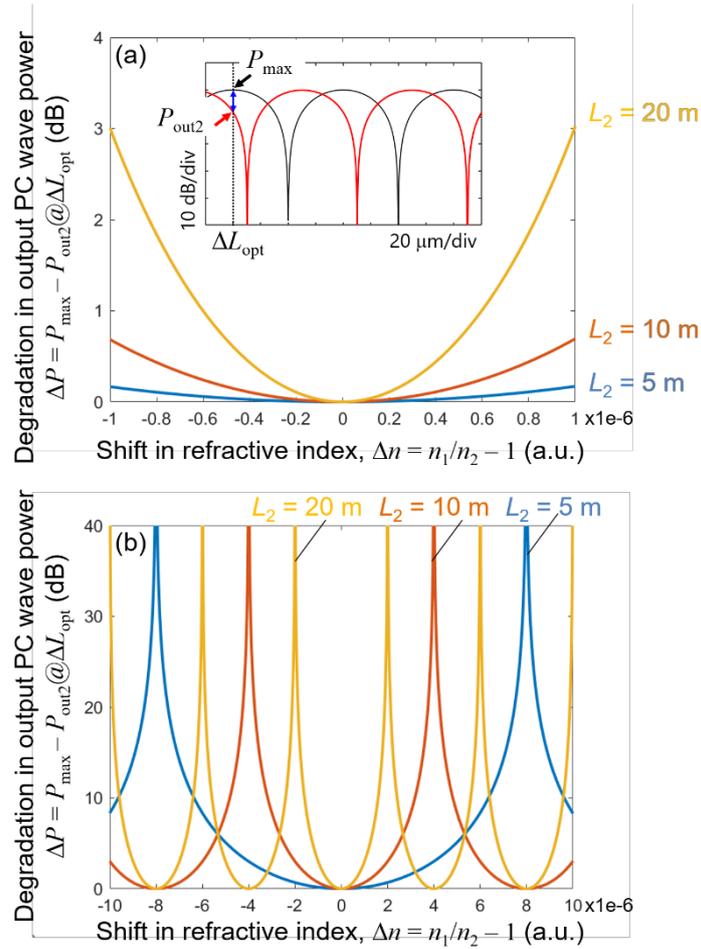


Fig. 3 Degradation ΔP in output PC wave power as function of shift Δn in refractive index. Blue, orange, and yellow lines represent the cases $L_2 = 5, 10, 20$ m, respectively. (a) Δn ranges from -1.0×10^{-6} to $+1.0 \times 10^{-6}$; (b) Δn ranges from -10.0×10^{-6} to $+10.0 \times 10^{-6}$

4. Dependence of output PC wave power on DE length and acceptable shift in refractive index

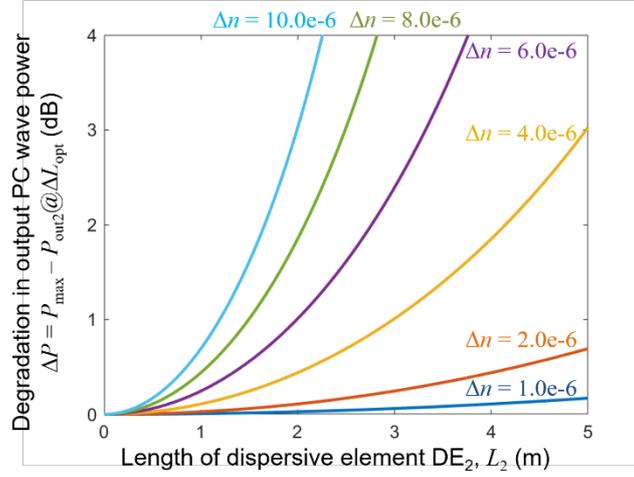


Fig. 4 Degradation ΔP in output PC wave power as function of DE_2 length, L_2 . Shift Δn in refractive index varies from $1.0e-6$ to $10.0e-6$

In this section, the dependence of the output PC wave power on DE_2 length and the acceptable shift in the refractive index is numerically investigated. Figure 4 depicts the degradation ΔP in the output PC wave power as a function of L_2 . Each curve indicates the shift Δn , ranging from $1.0e-6$ to $10.0e-6$. The degradation ΔP in the output PC wave power improves as L_2 reduces. This is because L_2 is the dominant factor of undesired phase shift, which is represented by the term $\Delta n(L_2 + \Delta L)$ in Eq. (5) where $\Delta L = 20 \mu\text{m}$, namely ΔL_{opt} . It is also understood that the optical waves traveling through DEs sense the shift in the refractive index Δn and are phase-shifted in proportion to DE_2 length L_2 . As a result, the PC wave partially outputs from port 1 because of the Sagnac loop, and the output PC wave power from port 2 is degraded. Based on this result, the acceptable shift in the refractive index for each L_2 can be determined when the acceptable degradation in the output PC wave power is known, and it would be useful for the design of the DFG-OPC.

Subsequently, the acceptable shift Δn_{tol} in the refractive index is calculated as a function of L_2 and presented in Fig. 5(a). Here, the acceptable degradation in the PC optical power is set to ΔP_{tol} , and the maximum Δn satisfying ΔP_{tol} at a certain value of L_2 is set to Δn_{tol} . In addition, the difference in temperature between the two DEs as a function of L_2 corresponding to Δn_{tol} is depicted in Fig. 5(b). The temperature difference ΔT between the two DEs is defined as $\Delta T = \Delta n_{\text{tol}} / (dn/dT)$ [°C]. Assuming that the DEs are single-mode fibers at $20 \text{ }^\circ\text{C}$, the thermo-optic coefficient dn/dT is set to $7.814e-6$ in these calculations, based on [29].

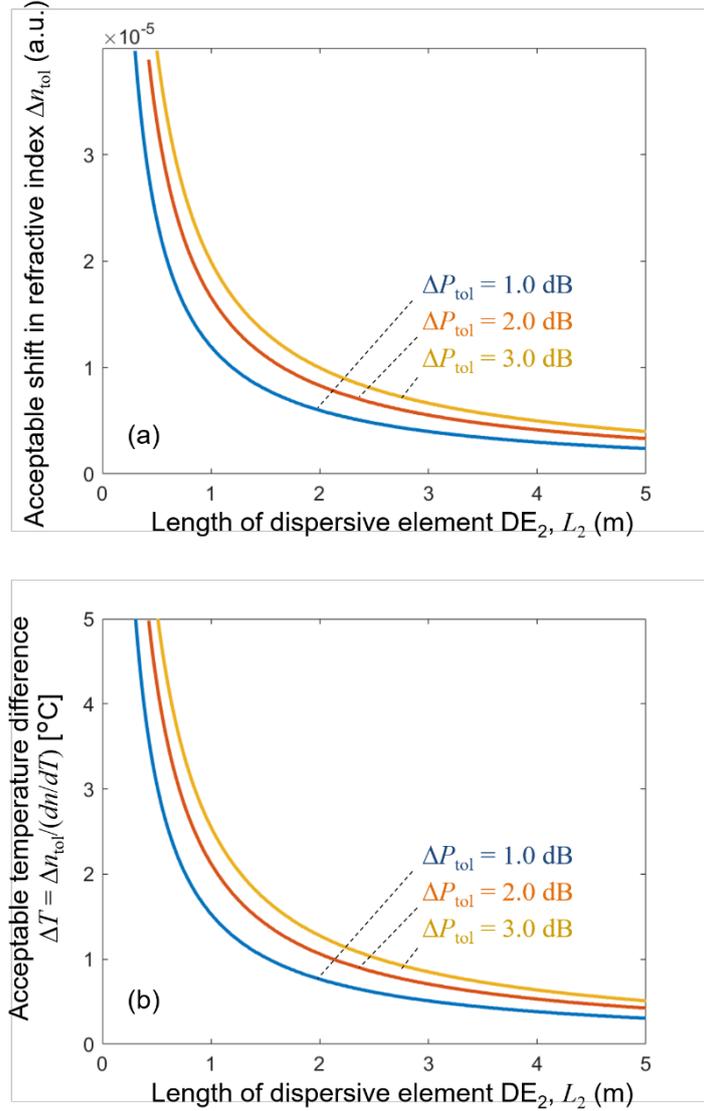


Fig. 5 (a) Acceptable shift in refractive index and (b) temperature difference as a function of DE_2 length, L_2

Figure 5(a) illustrates that Δn_{tol} increases as L_2 reduces. This is because the optical waves traveling through DEs partially sense the shift in the refractive index Δn when L_2 is comparatively shortened, and the undesired phase shift $\Delta n(L_2 + \Delta L)$ in Eq. (5) hardly increases by Δn . For example, if the acceptable degradation in the PC optical power is $\Delta P_{\text{tol}} = 1$ dB and $L_2 = 5$ m, $\Delta n_{\text{tol}} = 2.4 \times 10^{-6}$ corresponding to a temperature difference of 0.3 °C, as depicted in Fig. 5(b). This indicates that the temperature settings of DFG-OPCs have to be strictly managed for stable operation. Meanwhile, when $L_2 = 1$ m, $\Delta n_{\text{tol}} = 1.2 \times 10^{-5}$, which corresponds to a temperature difference of 1.5 °C. In this manner, the requirement of temperature control for the DFG-OPC is relaxed compared with the case when L_2 is longer. From these results, it was numerically clarified that the acceptable shift in the

refractive indexes between the DEs largely depends on L_2 . In response to this result, it was also found that it is essential to implement a DE length as short as possible to obtain stable output PC wave power from DFG-OPCs. These results would be useful for the design of DFG-OPCs.

Experimental verification of this study is one of the future works, and Δn control will play an important role in the experiment. The precise temperature control of the DE for the refractive index change must be required and would be a key issue. It also remains a challenge for further research to tune the refractive index dynamically. The thermoelectric cooler(TEC) could enable it. For example, the output power of the PC wave could be stabilized when the temperature of DEs is adaptively controlled with TECs in order that the monitored output PC wave power becomes constant. Additionally, the relatively wide range of the refractive index change could also be achieved by the TEC array along the fiber. For small Δn , the TEC array would be partially used. In contrast, for large Δn , the TEC array would be totally used. It is also expected that the DFG-OPC circuit with Δn control applies to unique applications such as phase-sensitive amplification. In the meantime, novel optical nonlinear media, such as All-optical modulator [30] and Metal-Organic Framework [31] have been studied and have the possibility to show different characteristics from the conventional optical nonlinear medium such as a highly nonlinear optical fiber. The application of such novel optical nonlinear media to OPC will be an interesting topic for future research.”

5. Conclusions

In this study, the effect of shift in the refractive indexes between DEs on the output PC wave power of waveband-shift-free DFG-OPCs was analytically investigated. In Section 2, the shift Δn in the refractive index, which has not been considered in earlier studies, was introduced into the DFG-OPC model. The obtained formula showed that not only the difference in DE lengths, ΔL , but also Δn and the DE₂ length, L_2 , affect the output PC wave power of DFG-OPCs. In Section 3, the dependence of the output PC wave power on the shift in the refractive index was analytically calculated. The output PC wave power was varied according to Δn . Even for $\Delta n = 1.0e-6$, the degradation ΔP in the output PC power was 3 dB when $L_2 = 20$ m. In Section 4, the dependence of the output PC wave power on L_2 was numerically investigated. The acceptable value of the shift, Δn_{tol} , and the temperature difference ΔT were calculated as functions of L_2 . The value of Δn_{tol} increased as L_2 was reduced; therefore, the output PC wave power could be stabilized against changes in temperature. Using the results obtained in this study to design DFG-OPCs, their robustness could be improved.

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