

1 Effect of region-dependent viscoelastic properties on the TMJ articular disc
2 relaxation under prolonged clenching.

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18 **Keywords**

19 Clenching, TMJ, viscoelastic behavior, stress analysis, material model

20

21 **Abstract**

22 The disc of the temporomandibular joint (TMJ) is located between the mandibular
23 condyle and temporal bone, and has an important load-bearing and stress
24 absorbing function. The TMJ disc presents viscoelastic characteristics that are
25 largely dependent on its collagen fibre and proteoglycan composition and
26 organization. The purpose of this study is to investigate the possible effects of
27 region-specific dynamic viscoelastic properties on stress relaxation during
28 prolonged clenching.

29

30 Two finite element models were used to compare the stress distribution within the
31 TMJ disc, namely, one with uniform disc material property and another one with
32 region-specific disc material properties. Similar results were observed in both
33 models with slight differences in the location of maximum stress. Larger stresses
34 were observed in all cases for the model with uniform disc material property.
35 Moreover, the higher values for the model with uniform disc material property
36 appeared in the lateral region, while in the model with region-specific disc

1 properties, these values moved to the lateral and central region.

2

3 This investigation confirms that both models are sufficiently accurate to
4 investigate stress distribution in the TMJ disc, and, particularly, the model with
5 the region-specific disc material properties ensure better simulations of the TMJ
6 disc behaviour.

7

8

1 **1 Introduction**

2 The disc of the temporomandibular joint (TMJ) is located between the mandibular
3 condyle and temporal bone and has an important load-bearing, stress absorbing
4 and joint stabilizing function during various mandibular movements working also
5 as articular cartilage (Barrientos et al., 2016, 2020; Fernández et al., 2013;
6 Tanaka et al., 2008; Eiji Tanaka & van Eijden, 2003). As sliding and rotating with
7 slightly lateral excursion occur simultaneously between articulating surfaces, the
8 TMJ disc is subjected to a multitude of different loading modes, according to the
9 region, and undergoes a deformation commensurate with its material properties
10 (Tanaka & van Eijden, 2003).

11 Like other articular cartilages, the TMJ disc exhibits not only elastic but also
12 viscous characteristics. The viscoelastic properties are mainly the result of fluid
13 flow into and out of the disc (Detamore & Athanasiou, 2003; Tanaka & van Eijden,
14 2003). The disc contains variable amounts of cells and an extracellular matrix
15 including macromolecules and fluid. These macromolecules consist mainly of
16 collagen (85-90%) and proteoglycans (10-15%) (Nakano and Scott, 1989;
17 Sindelar et al., 2000). The viscoelastic properties of the disc are largely
18 dependent on its collagen fibre and proteoglycan composition and distribution
19 and on their interaction with the tissue fluid (Detamore et al., 2005; Scapino et al.,
20 1996). It is also acknowledged that there are regional contrasts among the
21 distribution of collagen fibres and proteoglycans in the TMJ disc (Detamore et al.,
22 2005; Mizoguchi et al., 1998; Tanaka and van Eijden, 2003). This configuration
23 might allow the TMJ components to withstand the complicated compressive,
24 tensile and shear stress distribution prevailing during its function (del Pozo et al.,
25 2002).

26 Until now, numerous studies have been performed to determine the regional
27 difference of the dynamic viscoelastic properties of the TMJ disc (Fernández et
28 al., 2013; Tanaka et al., 2006). Fernández et al. (2013) indicates that the dynamic
29 viscoelastic properties are region-specific and depend on the loading frequency,
30 thus having important implications for the transmission of load to the TMJ.
31 Furthermore, the regional difference of the dynamic viscoelastic properties of the
32 TMJ disc might contribute to proper energy dissipation and stress absorption in
33 the TMJ during stress relaxation (Detamore & Athanasiou, 2003; Hattori-Hara et
34 al., 2014; Tanaka et al., 2014).

1 On the other hand, the information about the region-specific dynamic viscoelastic
2 parameters often makes difficult to fit a reasonable mechanical material model of
3 the disc that could be used for further calculation on the TMJ, such as numerical
4 models constructed with the finite element method. In this line, for **previous**
5 **studies** of TMJ stress analyses, only one set of viscoelastic parameters has been
6 commonly used for the TMJ disc (Abe et al., 2013; Barrientos et al., 2020;
7 Donzelli et al., 2004; Hattori-Hara et al., 2014; Hirose et al., 2006; Koolstra & van
8 Eijden, 2005; Pérez del Palomar & Doblaré, 2006; Tanaka et al., 2004), and no
9 study has been reported in which the region-specific material properties of the
10 TMJ disc were adopted to stress analyses with a finite element model of the TMJ.
11 The purpose of this study was to investigate the possible effects of region-specific
12 dynamic viscoelastic properties of the TMJ disc on stress relaxation during
13 prolonged clenching. A finite element model of the TMJ based on magnetic
14 resonance (MR) images from one healthy subject was constructed, and the
15 distributions of stresses in the TMJ disc during prolonged clenching in different
16 loading direction were analysed using a finite element model of the TMJ with the
17 dynamic compressive properties in the five different regions of the TMJ disc. After
18 that, a comparison between the behaviour of the disc using uniform material
19 property and the region-dependent disc properties was performed.

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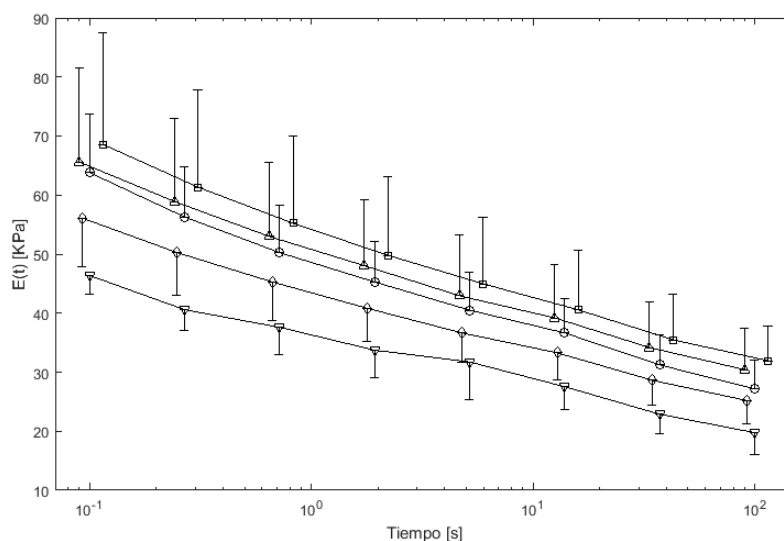
1 2 Materials and Methods

2 The current investigation involved the development of a finite element model
3 (FEM) in ABAQUS (Simulia, Dassault Systemes), in which the mechanical
4 viscoelastic properties of the different regions of the TMJ disc were implemented.
5 According to Fernández et al. (2013), five regions were selected and the region-
6 specific relaxation moduli were obtained. This modelling allowed the analysis of
7 the effects of region-specific viscoelastic properties of the TMJ disc on stress
8 relaxation during prolonged clenching.

9

10 2.1 Materials

11 To obtain the region-specific mechanical properties of the disc, experimental data
12 from Fernández et al. (2013) was collected. In order to obtain the relaxation
13 moduli of the five regions, the Ninomiya-Ferry algorithm (Ninomiya and Ferry,
14 1959) was applied using MATLAB. Although a wide variety of methods can be
15 used to performed the conversion between time-domain and frequency-domain,
16 Ninomiya-Ferry was selected due to the good balance that it presents between
17 the accurate results and the low calculus capacity needed (Emri et al., 2005). The
18 region-specific relaxation moduli are presented in Figure 1 and the numerical
19 values are given in appendix A: (Tables A1-A5).



20

21 Figure 1. Relaxation modulus for each region: Posterior (\square), Anterior (Δ), Central
22 (\circ), Medial (\diamond) and Lateral (∇).

23

24 In order to use the region-specific relaxation moduli $E(t)$ in FEM, the curves were

1 fitted using the linear viscoelastic generalized Maxwell model (Chen, 2000;
 2 Tschoegl, 2012).

$$E(t) = E_0 \left[1 - \sum_{i=1}^{n_t} e_i \left(1 - \exp\left(-\frac{t}{\tau_i}\right) \right) \right] \quad (1)$$

3
 4 where τ_i are the times, e_i the modulus ratios and E_0 is the instantaneous
 5 modulus. The material model was fitted using an optimized Prony series method
 6 (Barrientos et al., 2019). This method optimizes the best locations for both times
 7 (τ_i) and modulus ratios (e_i) in order to minimize the number of prony terms
 8 necessary in the material model. For the present relaxation curves (see Figure 1)
 9 and based on the numerical errors in the fittings for the homogenous and optimal
 10 discrete time distributions (Barrientos et al., 2019), the optimized model is
 11 obtained when 3 prony series terms are used being the error 0.04%. The
 12 viscoelastic models (see Eq. (1)) fitted for each region are presented in appendix
 13 A (Tables A6-A10).

14

15 2.2 Finite element model

16 To examine the stress relaxation during prolonged clenching in the TMJ disc, a
 17 finite element model of the TMJ, based on Barrientos et al. (2020), was
 18 implemented in ABAQUS (Simulia, Dassault Systemes).

19 In order to introduce the region-specific mechanical material properties, the disc
 20 from Barrientos et al. (2020), modelled as 3D deformable solid, had to be
 21 modified. On the other hand, temporal bone and cartilages were modelled as
 22 discrete rigid solids (Barrientos et al., 2020). Finally, both condylar and temporal
 23 cartilages were modelled using skin shell elements with linear elastic properties
 24 (see Table 1).

25

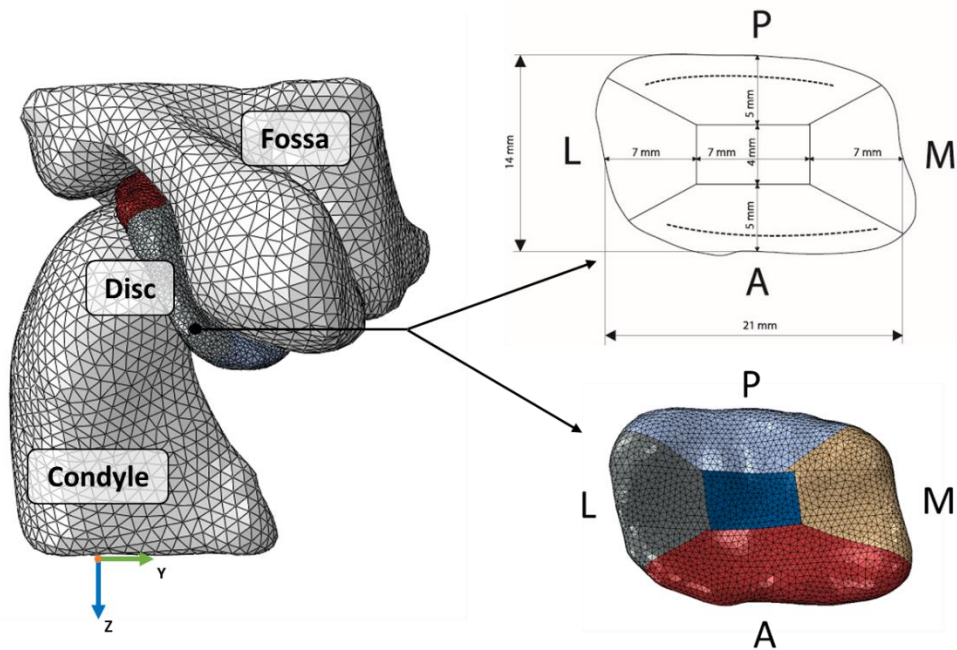
26 Table 1. Material properties for the cartilages (from Tanaka et al., 2014)

Model part	Young Modulus, E [MPa]	Poisson ratio, ν
Condylar cartilage	0.8	0.3
Temporal cartilage	1.5	0.3

27

28 As a first step, the geometry of the disc was split into five regions: anterior (A),
 29 posterior (P), Lateral (L), Medial (M) and Central (C). The regional division,

1 showed in Figure 2, was assumed in agreement with the experimental
 2 methodology used to obtain the dynamic viscoelastic parameters (Fernández et
 3 al., 2013), with the morphology of the articular disc and with the viability of the
 4 modelling procedure. Additionally, the viscoelastic material models previously
 5 obtained (section 2.1 Materials) were directly assigned to each corresponding
 6 region. Finally, a mesh sensitivity analysis was carried out and considering the
 7 convergence of the results and the computational costs, linear tetrahedral
 8 elements of approximately 0.5 mm size were chosen.



9
 10 Figure 2. Regions created in the FE model for defining each material region.

11
 12 In order to avoid the influence and uncertainties in the contacts between model
 13 parts, TIE contacts were used. In this type of contacts, nodes on the slave surface
 14 have the same value of displacement as the point on the master surface that it
 15 contacts. (Simulia, 2016)

16 Finally, the region-specific FEM was also used for comparison with the case of
 17 uniform disc material properties. With this aim, the same material was assigned
 18 for the five regions described previously. The material used for the uniform
 19 mechanical properties disc was retrieved from Barrientos et al. (2020). The Prony
 20 coefficients for the generalized Maxwell model (see Eq. (1)) are presented in
 21 Table 2.

1

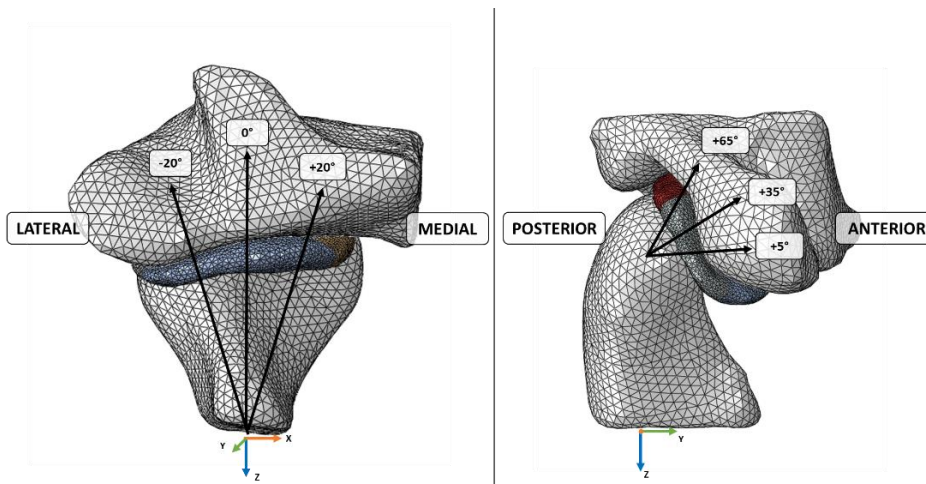
2 Table 2. Mechanical properties used for the uniform disc case (Barrientos et al.,
3 2020)

Poisson ratio, ν	0.4
Young Modulus, E_0 [MPa]	0.18
Prony terms	
e_1	0.5733
τ_1	0.0384
e_2	0.1223
τ_2	0.4925
e_3	0.0818
τ_3	6.3499
e_4	0.0926
τ_4	106.4815

4

5 2.3 Simulations

6 In regard to the boundary conditions, the movement of the temporal bone was
7 restricted, while only displacement of the condyle was allowed to simulate the
8 clenching conditions.



9

10 Figure 3. Illustration of the condylar directional loading applied in the simulation.

11

12 The loading conditions were defined taken into account the five regions
13 considered in the disc (see Figure 2). For each define loading angle, the
14 necessary displacements for applying a 10% compression strain in the disc were

1 estimated. The values for the displacements applied to the reference point of the
 2 condyle according to the model coordinate system (see Figure 3) in the medio-
 3 lateral direction are presented in Table 3.

4

5 Table 3. Loading angles used in the medio-lateral direction. (see Figure 3)

Angle	U_x [mm]	U_y [mm]	U_z [mm]
-20°	-0.035	0.096	-0.096
0°	0	0.1	-0.1
20°	0.035	0.096	-0.096

6

7 On the other hand, three loading angles as representative ranges of the TMJ
 8 movement were considered for the antero-posterior direction (see Table 4).
 9 These loading angles (see Figure 3) were selected according to the study of Beek
 10 et al. (2000).

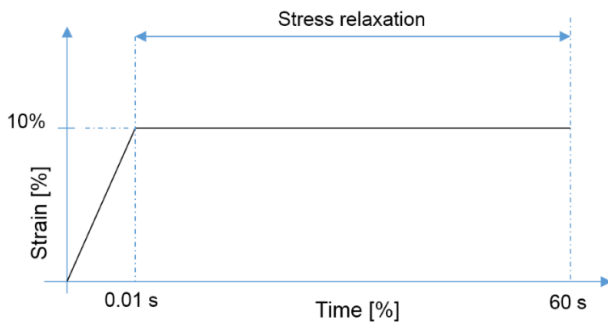
11

12 Table 4. Loading angles used in the antero-posterior direction (see Figure 3).

Angle	U_x [mm]	U_y [mm]	U_z [mm]
65°	0	0.060	-0.128
35°	0	0.116	-0.081
5°	0	0.141	-0.012

13

14 The loading conditions applied and the simulation loading steps were exactly the
 15 same in both uniform properties and region-specific properties models. The
 16 simulations of prolonged clenching were made in different steps (Barrientos et al.,
 17 2020), described as the loading conditions illustrated in Figure 4.



18

19 Figure 4. Loading conditions for simulation of prolonged clenching.

1

2

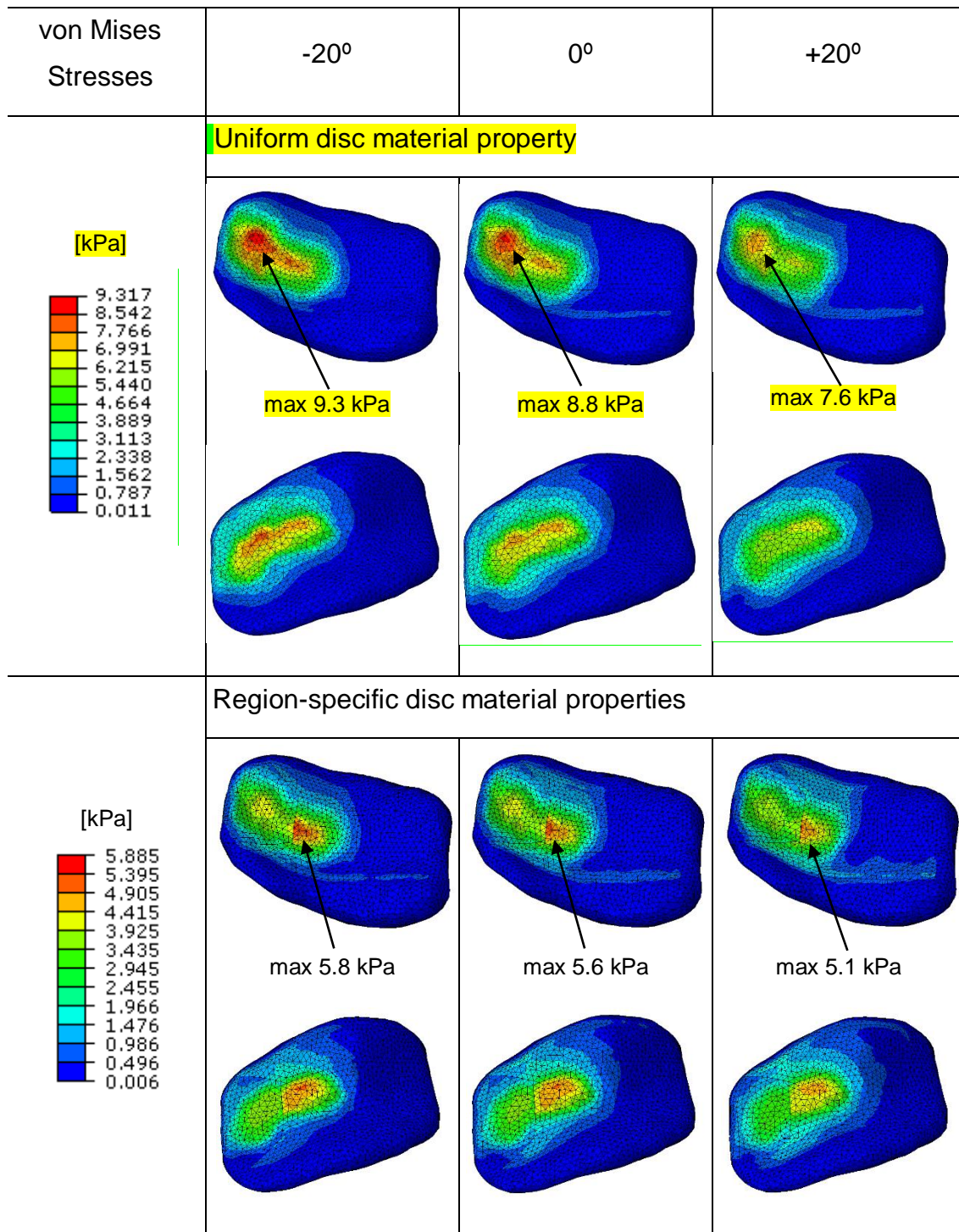
1 **3. Results**

2 In this study, the stress distribution on the TMJ disc of both models during
3 prolonged clenching are shown at three different instances of time: $t = 0.1$ s,
4 which corresponds to the first available data of the specific-region material ; $t = 1$
5 s, which represents an approximate relaxation ratio of about 50% in the material;
6 and $t = 60$ s at the end of the relaxation step. Moreover, variations in the results
7 due to the loading direction are studied.

8

9 **3.1 Medio-lateral direction**

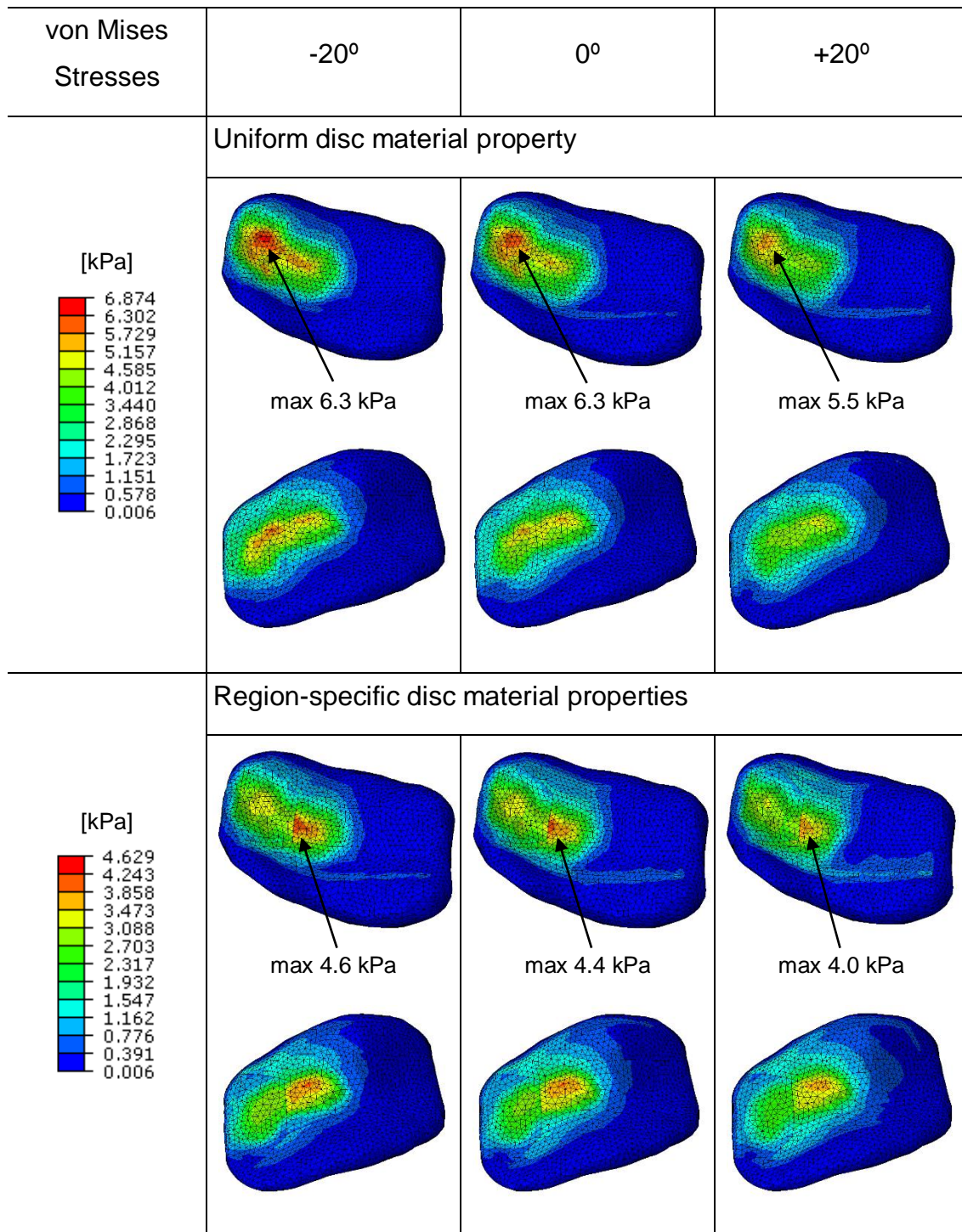
10 Firstly, von Mises stress results of the both models in the medio-lateral direction
11 are presented. The largest von Mises stresses on the surface of the TMJ disc
12 due to medio-lateral loading variations were observed when the loading was
13 applied at -20° direction. On the other hand, the lowest stresses were obtained
14 when the loading direction was set to $+20^\circ$ as the stress distribution was more
15 uniform.



1 Figure 5. von Mises stresses in the disc at $t = 0.1$ s
2
3 In Figure 5, the largest von Mises stresses at $t = 0.1$ s were found in the model
4 with uniform disc material property with a value of 9.3 kPa, whereas 5.8 kPa were
5 obtained in the model with region-specific disc properties. This difference
6 represents a reduction in stress of approximately 38% between models. On the
7 other hand, as shown in Figure 6, the maximum stress values at $t = 1$ s were 6.3

1 kPa for the model with uniform disc property and 4.6 kPa for the model with
2 region-specific disc properties, which represents a reduction in stress of
3 approximately 28%. In addition, stresses after relaxation ($t = 60$ s) in both models
4 are presented in Figure 7. Higher stress values are also obtained for the model
5 with uniform disc property. The maximum stress values were 4.2 kPa for the
6 model with uniform disc property and 2.9 kPa for the model with region-specific
7 disc properties, which represents a reduction in stress of approximately 30%
8 between models.

9
10



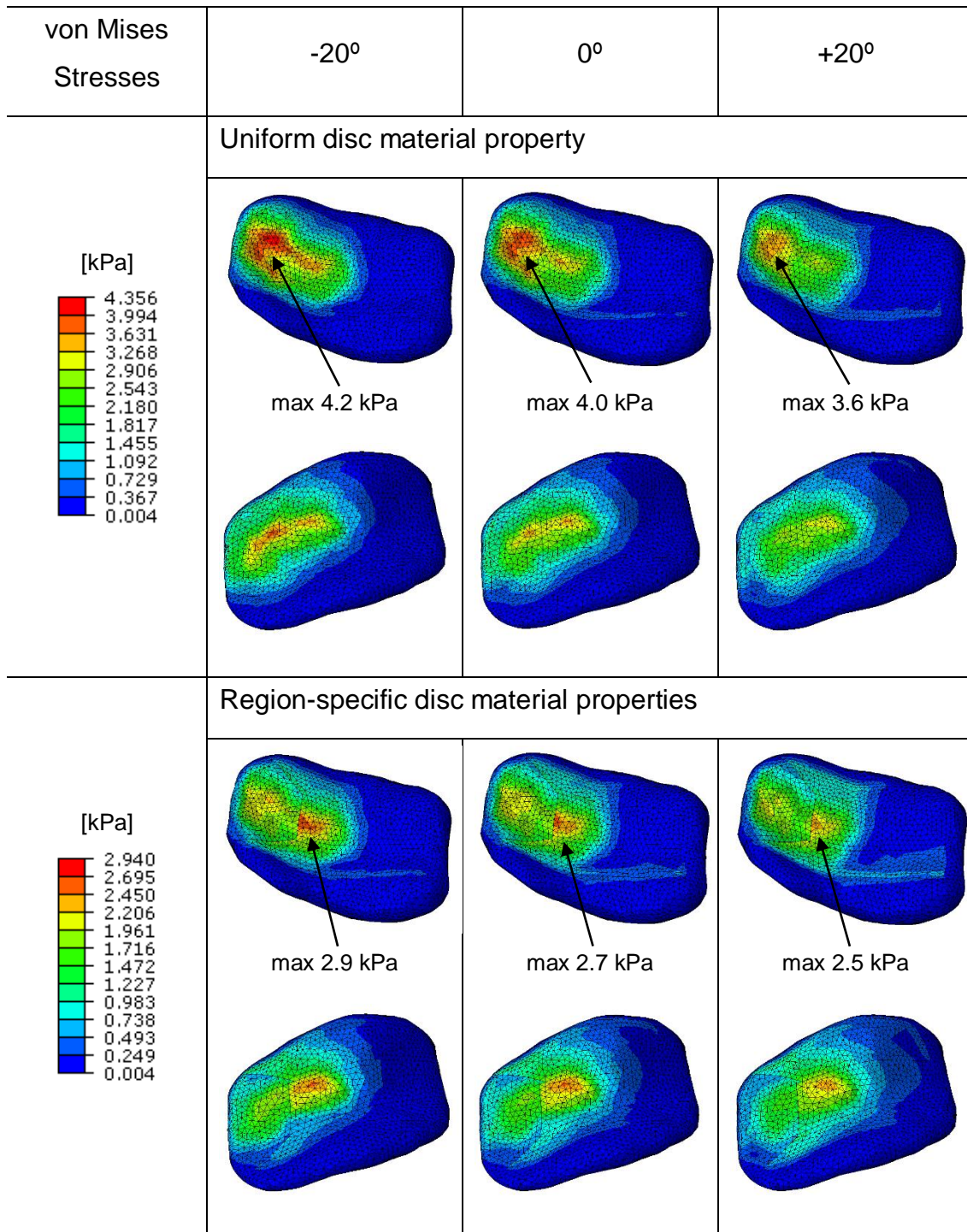
1 Figure 6. von Mises stresses in the disc at $t = 1$ s.

2

3 Concerning the location of the largest von Mises stresses, in the model with
 4 uniform disc property the largest von Mises stresses were located in the lateral
 5 region, while, in the model with region-specific disc properties, were also in the
 6 lateral region but closer to central region of the disc, both at $t = 0.1$ s and $t = 60$
 7 s. (See Figures 5 and 7). However, at $t = 1$ s, as it can be seen in Figure 6, stress

1 distribution was similar to those previously commented with a slight increment in
 2 stress towards the anterior zone.

3



4 Figure 7. von Mises stresses in the disc at t = 60 s.

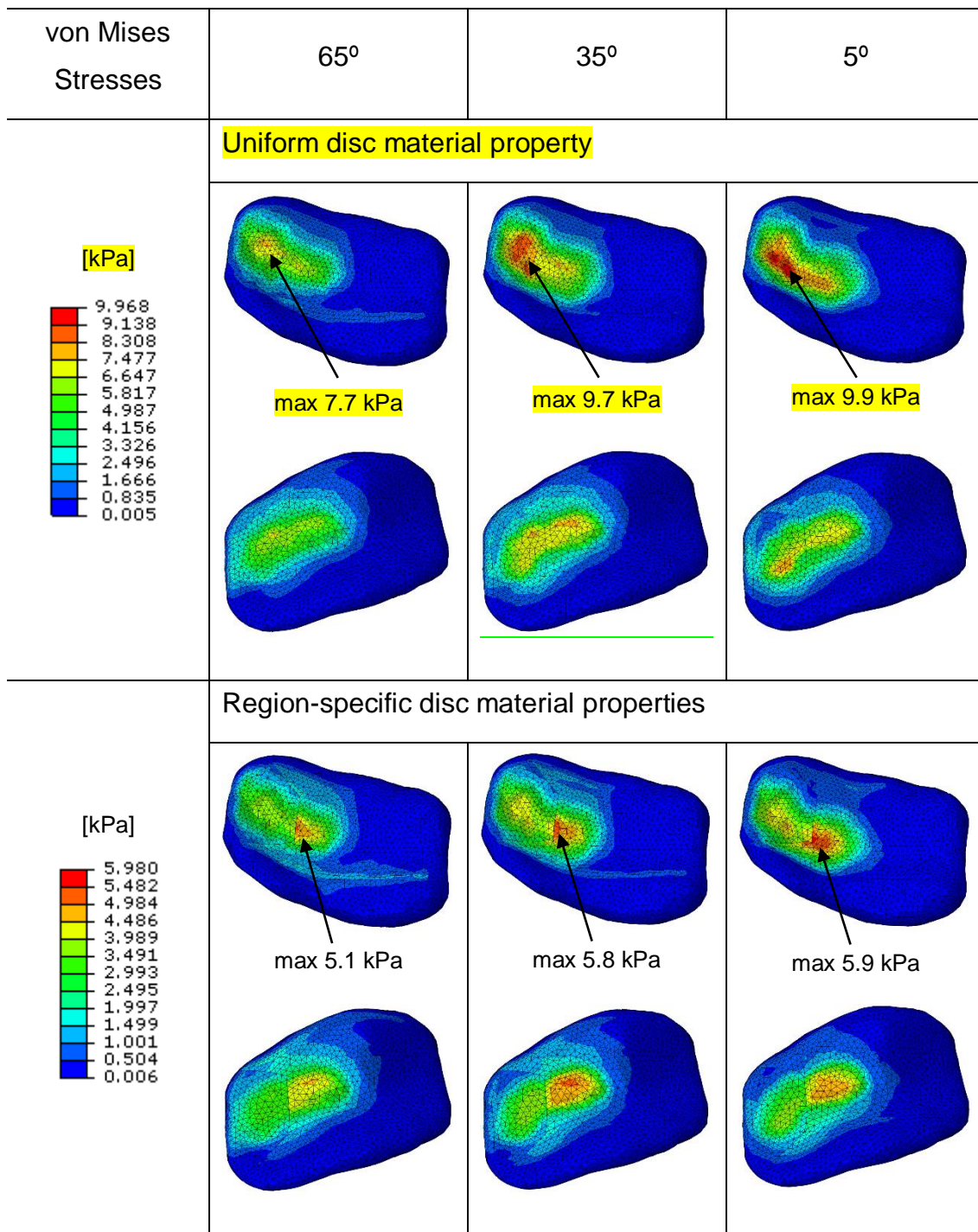
5

6 Regarding the stress relaxation ratio at t = 60 s, in these simulations, the value
 7 was 54% for the model with uniform disc property. On the other hand, the stress

1 relaxation ratio was 50% for the model with region-specific disc properties.

2 **3.2 Antero-posterior direction**

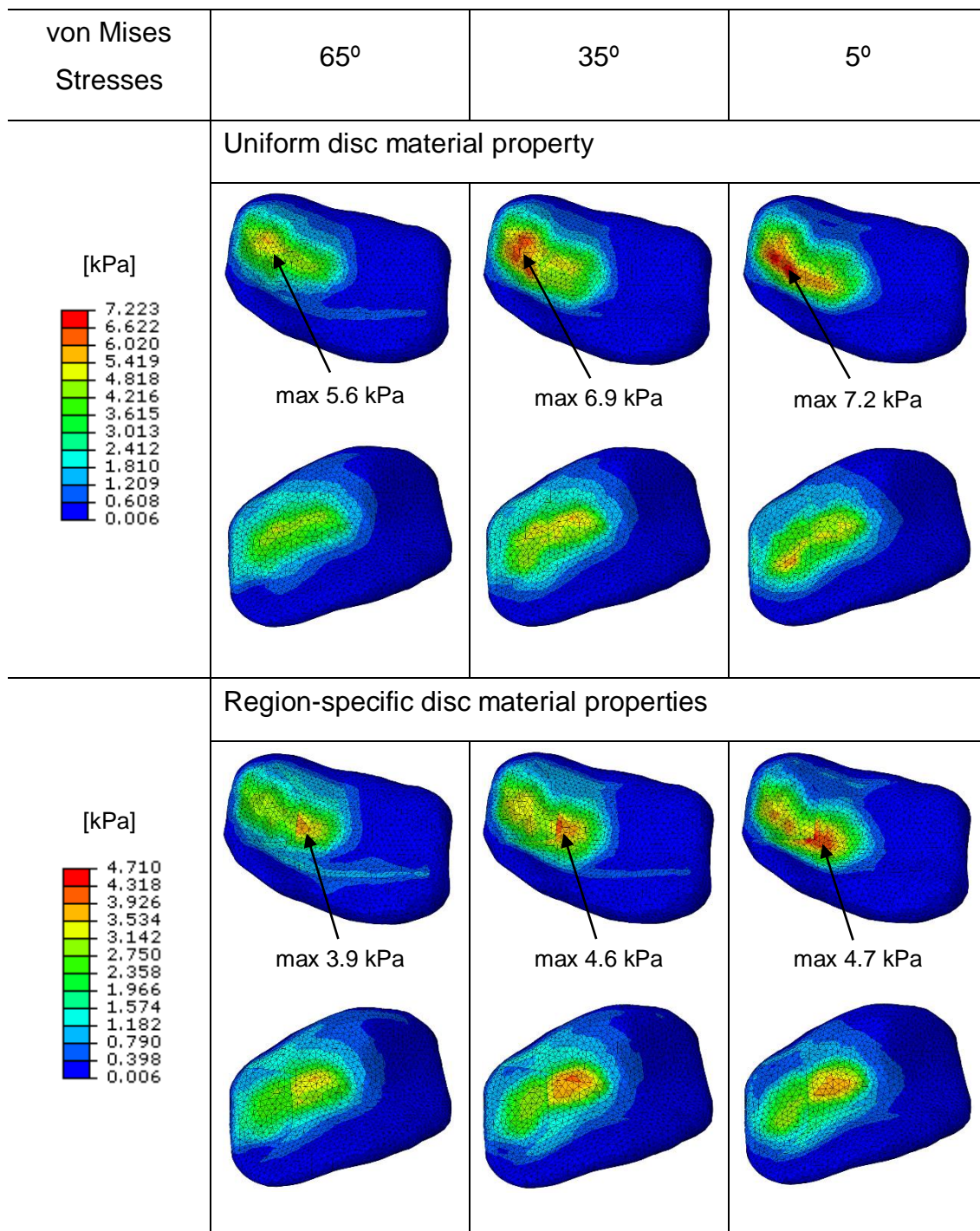
3 In Figures 8-10, von Mises stress results of both models in the antero-posterior
 4 direction are presented. In these simulations, the largest von Mises stresses on
 5 the surface of the TMJ disc were observed when the loading was applied in +5°
 6 direction, irrespective of the simulated time.



7 Figure 8. von Mises stresses in the disc at **t = 0.1 s.**

8

1 According to Figure 8, the highest stresses at $t = 0.1$ s were found in the model
2 with uniform disc property with a value of 9.9 kPa, whereas 5.9 kPa was obtained
3 in the model with region-specific disc properties, which represents a reduction in
4 stress of approximately 40% between models. On the other hand, as seen in
5 Figure 9, the largest stress at $t = 1$ s was presented in the model with uniform
6 disc property with a value of 7.2 kPa, whereas 4.7 kPa was obtained in the model
7 with region-specific disc properties, which represents a reduction in stress of
8 approximately 35% between models. Moreover, the stresses at $t = 60$ s were
9 presented in Figure 10. Higher stress values were also obtained for the model
10 with uniform disc property, being the maximum stress values 4.7 kPa for the
11 model with uniform disc property and 3.2 kPa for the model with region-specific
12 disc properties, which represents a reduction in stress of approximately 32%
13 between models.



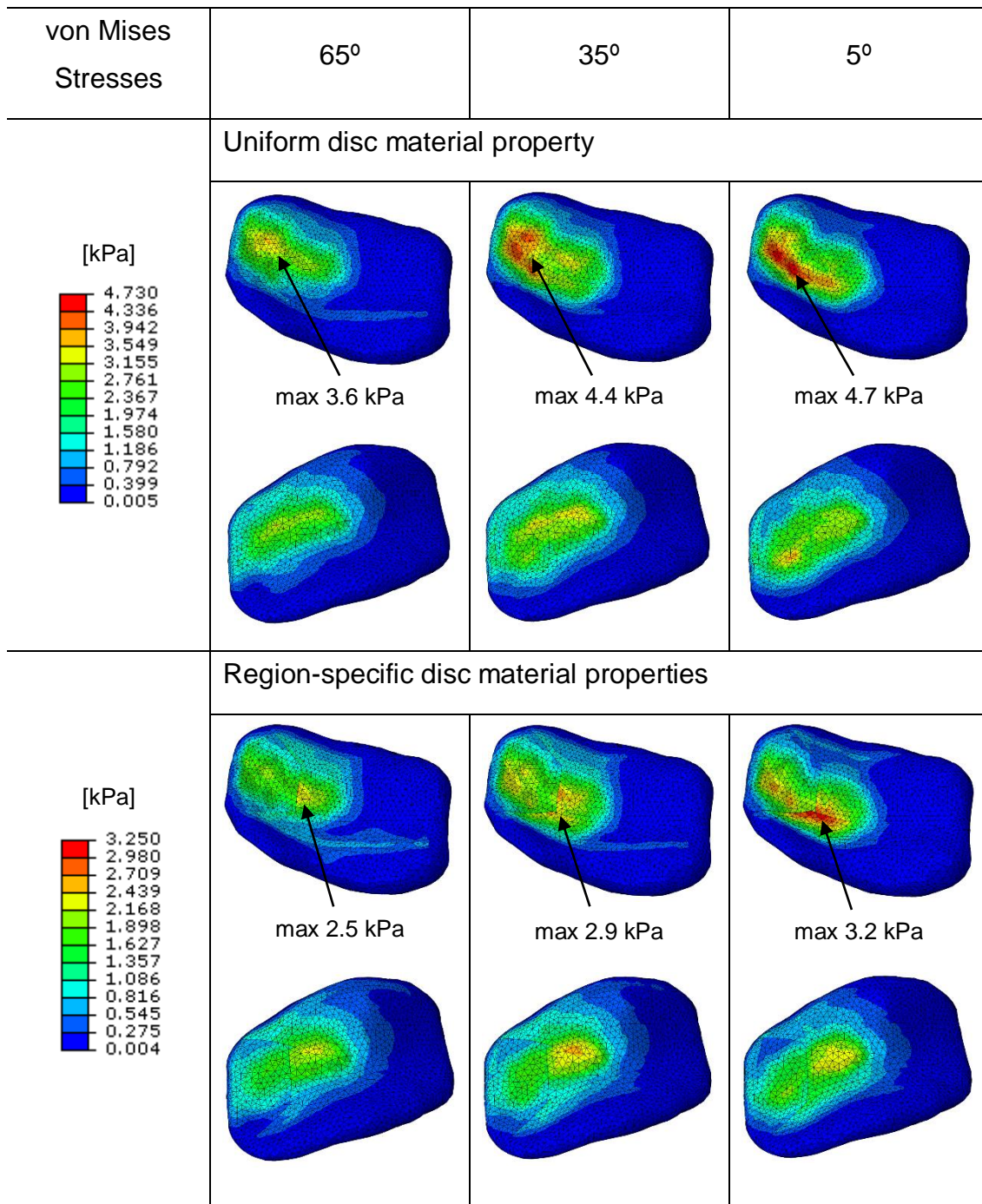
1 Figure 9. von Mises stresses in the disc at $t = 1$ s.

2

3 Concerning the stress location, as in the medio-lateral direction, the largest von
 4 Mises stresses were located in the lateral region for the model with uniform disc
 5 property, whereas in the model with region-dependent material properties the
 6 largest stresses were located in the central region. Moreover, the influence of the
 7 variation of the loading angles in the antero-posterior direction was observed at
 8 +5 direction, being the largest stresses, in both models, closer to the anterior

1 region, at the three instances of time.

2



3 Figure 10. von Mises stresses in the disc at $t = 60$ s.

4

5 Regarding stress relaxation ratio at 60 s, in these simulations a value of 53% was
6 found for the model with uniform disc property. On the other hand, the stress
7 relaxation ratio was 46% for the model with region-specific disc properties. Both
8 were closed to the values found in the medio-lateral direction.

1 Finally, comparing the effects of the angle variation for the medio-lateral direction
2 and the antero-posterior direction, as it was mentioned, the largest stress was
3 found at -20° for the medio-lateral and at $+5^\circ$ in the antero-posterior. Between
4 both, the larger stress was always found at $+5^\circ$ on the antero-posterior direction.
5
6

1 Discussion

2 It is well-known that the TMJ disc contributes to control loads exerted by various
3 mandibular movements, and the regulated loads contribute to growth,
4 development and maintenance of the TMJ components (Stegenga et al., 1989).
5 Since the TMJ disc has viscoelastic behavior, it enables stress reduction and
6 distribution in the TMJ components and energy dissipation within the joint tissues
7 (Guerrero Cota et al., 2019; Tanaka et al., 1999; Tanaka & van Eijden, 2003). The
8 compressive moduli mainly depend on the density of the proteoglycans,
9 especially large chondroitin sulfate, while the tensile moduli mainly depend on the
10 amount and orientation of collagen fibers (Detamore & Athanasiou, 2003; Tanaka
11 & van Eijden, 2003). Furthermore, corresponding to the evidence that there is
12 regional dissimilarity in the distribution of proteoglycans and glycosaminoglycans
13 in the TMJ disc (Mizoguchi et al., 1998; Sindelar et al., 2000), the region-specific
14 viscoelastic properties of the TMJ disc have been reported (Barrientos et al.,
15 2019; Chen et al., 2020; Fernández et al., 2013; Guerrero Cota et al., 2019). It
16 has been demonstrated the similarity between the regional distributions of the
17 amount of proteoglycans and the compressive moduli, which supported the
18 biomechanical data of the association between chondroitin sulfate presence and
19 compressive property of the TMJ disc (Fernández et al., 2013; Guerrero Cota et
20 al., 2019). Taken these considerations, the region-specific mechanical properties
21 of the TMJ disc should be used for stress analysis in the TMJ by using a finite
22 element models; however, limited information was available about the effect of
23 region-specific mechanical properties of the TMJ disc on the stress distribution in
24 the TMJ. To our best knowledge, this is the first study in which the difference of
25 stress distribution in the TMJ finite element models with the region-specific moduli
26 and with a representative single modulus was examined.

27

28 Data obtained in previous studies using single disc material property (Barrientos
29 et al., 2020) indicated that largest von Mises stresses were located at the lateral
30 region. In addition, larger von Mises stress was found when the loading was
31 applied in the -20° medio-lateral direction. Nonetheless, when the loading was
32 applied in 20° medio-lateral direction, von Mises stress was distributed over a
33 wider area. Moreover, larger von Mises stress was found at $t = 0.01$ s, In this
34 study, the same observations seen by Barrientos et al. (2020) were found for the

1 model with single disc material property in the medio-lateral direction, in terms of
2 regional location of the largest von Mises stress, variations on stresses with the
3 loading direction and relaxation ratio. Nonetheless, different values of stress were
4 found due to the differences on the type of contacts and the elements of the disc
5 used. On the other hand, new observations were found for the model with region-
6 specific disc properties, in terms of stresses and its distribution in the different
7 regions.

8
9 In the present study differences in stresses were encountered between the model
10 with uniform disc material property and the model with region-specific properties
11 (see Section 3). Even though the differences are dependent on the loading
12 direction and the instance of time, lower values were always obtained in the
13 model with region-specific disc properties. The present results also demonstrated
14 that relatively larger von Mises stresses were present at the anterior, lateral, and
15 central regions of the TMJ disc during prolonged clenching irrespective of time.
16 Previous studies showed stress distributions in the TMJ disc were speculated
17 from anatomical and biochemical findings in the TMJ disc (Scapino et al., 2006;
18 Singh & Detamore, 2009; Tanaka et al., 1994). Anatomical studies with cadavers
19 indicate that marked thinning and perforation of the disc were more frequently
20 found in the anterior, central and lateral regions while the pathological hiascent
21 was often detected in the posterior region, especially at the disc-retrodiscal tissue
22 border (Touré et al., 2005). In addition to that, from the biochemical aspect, the
23 glycosaminoglycan, associated with compressive stresses in the healthy TMJ
24 disc, was distributed greatly in the anterior, central and lateral regions of the TMJ
25 disc but not in the posterior region (Detamore and Athanasiou, 2003; Guerrero
26 Cota et al., 2019; Lin et al., 2018). In both models, the distribution of the
27 compressive stresses in the TMJ disc was similar. Furthermore, Wang et al.,
28 (2008), using cadavers, investigated whether the TMJ disc responses to
29 dysfunctional occlusal changes by an increase in thickness, and demonstrated
30 that the TMJ disc has the ability to adapt to alteration of the space between
31 condyle and fossa caused by occlusal changes. This means healthy TMJ disc is
32 likely to show a uniform distribution of stresses on its articular surfaces. Taken
33 these considerations, both models were confirmed to have sufficient physical and
34 biomechanical equivalence to investigate the microcircumstances within the TMJ,

1 and especially the model with the region-specific disc properties might simulate
2 better the TMJ.

3

4 Obviously, the assumptions and simplifications underlying the biomechanical
5 models of the human TMJ should be taken into account when interpreting its
6 predictions (Breedveld, 2004). Furthermore, the results obtained in the present
7 study cannot be immediately transferred to clinical practice without further serious
8 considerations. With respect to the present analysis, the following remarks have
9 to be noticed. First, the material properties of the TMJ disc and cartilage were
10 modelled according to experimental data obtained from porcine TMJ (Barrientos
11 et al., 2020; Fernández et al., 2013), because no reliable material properties for
12 human are available in the previous literatures. While human discs possessed
13 properties distinct from those of the other species, porcine discs are considered
14 to be close to that of humans, suggesting that the pig may be a suitable animal
15 model for TMJ bioengineering efforts (Herring, 2003; Kalpakci et al., 2011).
16 Second, the tensile and shear properties of the TMJ disc were different from the
17 compressive one (Tanaka and van Eijden, 2003). Therefore, the TMJ disc could
18 be regarded as anisotropic materials. In the present study, the anisotropic
19 behaviour of the disc was not taken into account because the disc was subject to
20 compression during prolonged clenching irrespective of the loading direction
21 (Barrientos et al., 2020). Nevertheless, further study using an anisotropic disc
22 model should be performed in the future. Third, although biphasic or poroelastic
23 material model is commonly applied to express the material behaviour of articular
24 cartilage (Mow et al., 1984; Prendergast et al., 1996), we adopted the linear
25 viscoelastic generalized Maxwell model to express the biomechanical behaviour
26 of TMJ disc. Allen and Athanasiou (2006) demonstrated that since the TMJ disc
27 contains much less proteoglycans, a viscoelastic model is considered to be more
28 suitable for the TMJ disc. Koolstra et al. (2007) also described that although other
29 mechanical models based upon the poroelastic and biphasic theories could also
30 be fit to these data, these other models may have limitations when modelling the
31 mechanical response of the TMJ disc due to lower concentration of
32 glycosaminoglycans (GAGs). Lower GAG and proteoglycan concentrations are
33 likely to result in a reduced drag between the fluid and solid matrix (Allen and
34 Athanasiou, 2006). For this reason, we selected a viscoelastic model to represent

1 the TMJ disc as opposed to a poroelastic or a biphasic model. However, in the
2 future, a comparison study between linear and non-linear viscoelastic models
3 should be conducted. Finally, the model geometry was based on MRI data of only
4 one healthy patient. It is true that large variation exists among individuals and
5 there might be an interindividual difference in structure and function of
6 musculoskeletal systems including the TMJ. This implies a large difference in the
7 amount of TMJ stress among the models. Assuming the stress analysis as only
8 one healthy TMJ may be too simplified to for a quantitative analysis of TMJ stress,
9 the present study has to be considered as qualitative.
10

1 Conclusions

- 2
- 3 • The model with uniform disc material property presents higher stresses for
- 4 the same loading than those obtained using the model with region-specific
- 5 disc material properties.
- 6 • In medio-lateral direction, higher stresses were obtained for the -20°
- 7 loading direction in both models, whereas lower and more uniform
- 8 distributed stresses were obtained at 20°. In antero-posterior direction,
- 9 higher stresses were obtained for the +5° loading direction. Between
- 10 models, the largest stress was always found at +5° in the antero-posterior
- 11 direction.
- 12 • The highest von Mises stresses were induced in the lateral region for the
- 13 the model with uniform disc material property. Nevertheless, higher von
- 14 Mises stresses were also found in the lateral and central region for the
- 15 model with region-specific disc properties.
- 16 • Due to the loading variations at the antero-posterior direction, the highest
- 17 stresses were found in the lateral region but closer to the anterior region
- 18 for the model with uniform disc material property. However, the largest
- 19 stresses were induced in the central and anterior region for the model with
- 20 region-specific disc properties.
- 21 • A clinical implication from these findings is that an early approach to
- 22 parafunctional habit such as habitual one-sided chewing, bruxism, and
- 23 clenching would be desirable to reduce excessive stress in the specific
- 24 region of the disc.

1 **Acknowledgements**

2 The authors would like to express their gratitude to the Spanish Ministry of
3 Economy and Competitiveness for the financial support of the project
4 “Probabilistic prediction of damage and fatigue failure: application to components
5 and structures of polymeric materials” (DPI2016-80389-C22-2-R), as well as to
6 the CajAstur Fellowship-University of Oviedo’s 2011 programme.

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7
8

1 **Appendix A**

2 Tables with relaxation modulus obtained from Ninomiya-Ferry Conversion
3 (Ninomiya and Ferry, 1959) from Complex moduli (Fernández et al., 2013).

4 Note: $E(t)$ is the mean and E_{max} and E_{min} are the maximum and minimum limits
5 for each time interval.

6

7 Table A1: Anterior relaxation modulus

Time [s]	E [Pa]	E_{max} [Pa]	E_{min} [Pa]
0.1	65584	81503	49665
0.26827	58906	73057	44754
0.71969	52978	65583	40373
1.9307	48033	59246	36820
5.1795	42943	53190	32696
13.895	39205	48178	30231
37.276	34171	41936	26406
100	30437	37433	23442

8

9 Table A2. Central relaxation modulus

Time [s]	E [Pa]	E_{max} [Pa]	E_{min} [Pa]
0.1	63799	73665	53933
0.26827	56287	64859	47715
0.71969	50250	58220	42280
1.9307	45284	52232	38336
5.1795	40501	46988	34014
13.895	36652	42415	30888
37.276	31228	36415	26041
100	27178	32033	22322

10

1 Table A3. Lateral relaxation modulus

Time [s]	E [Pa]	E _{max} [Pa]	E _{min} [Pa]
0.1	46379	49502	43284
0.26827	40583	44745	36993
0.71969	37601	41777	32982
1.9307	33727	38478	29030
5.1795	31734	36684	25407
13.895	27541	31939	23738
37.276	22882	27203	19529
100	19756	24206	15961

2

3 Table A4. Medial relaxation modulus

Time [s]	E [Pa]	E _{max} [Pa]	E _{min} [Pa]
0.1	56108	64386	47830
0.26827	50254	57463	43045
0.71969	45290	51797	38783
1.9307	40828	46360	35297
5.1795	36643	41605	31681
13.895	33285	37875	28694
37.276	28635	32836	24433
100	25184	29120	21247

4

5 Table A5. Posterior relaxation modulus

Time [s]	E [Pa]	E_{\max} [Pa]	E_{\min} [Pa]
0.1	68567	87481	49653
0.26827	61336	77749	45143
0.71969	55212	70050	40202
1.9307	49788	63081	36538
5.1795	44968	56208	33206
13.895	40563	50687	30619
37.276	35482	43261	26882
100	31934	37776	24092

1

2 Tables with linear viscoelastic models for each region

3

4 Table A6. Posterior region Prony coefficients

Poisson ratio, ν	0.4
Young Modulus, E_0 [MPa]	0.0655
Prony terms	
e_1	0.2621
τ_1	0.6795
e_2	0.1484
τ_2	9.6169
e_3	0.1589
τ_3	64.1328

5

6 Table A7. Anterior region Prony coefficients

Poisson ratio, ν	0.4
Young Modulus, E_0 [MPa]	0.0637
Prony terms	
e_1	0.2243
τ_1	0.5059
e_2	0.1152

τ_2	2.5165
e_3	0.2444
τ_3	31.1899

1

2 Table A8. Central region Prony coefficients

Poisson ratio, ν	0.4
Young Modulus, E_0 [MPa]	0.0463
Prony terms	
e_1	0.2458
τ_1	0.5344
e_2	0.1934
τ_2	14.3452
e_3	0.1551
τ_3	49.2614

3

4 Table A9. Lateral region Prony coefficients

Poisson ratio, ν	0.4
Young Modulus, E_0 [MPa]	0.0561
Prony terms	
e_1	0.2039
τ_1	0.5387
e_2	0.1182
τ_2	2.4615
e_3	0.2384
τ_3	30.9592

5

6 Table A10. Medial region Prony coefficients

Poisson ratio, ν	0.4
Young Modulus, E_0 [MPa]	0.0685
Prony terms	
e_1	0.2291
τ_1	0.5702
e_2	0.1074

τ_2

3.6769

e_3

0.2056

τ_3

30.4911

1
